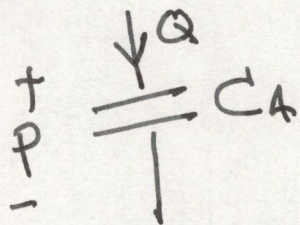
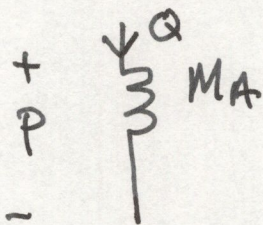


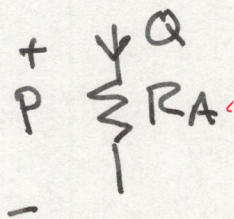
Acoustic Elements

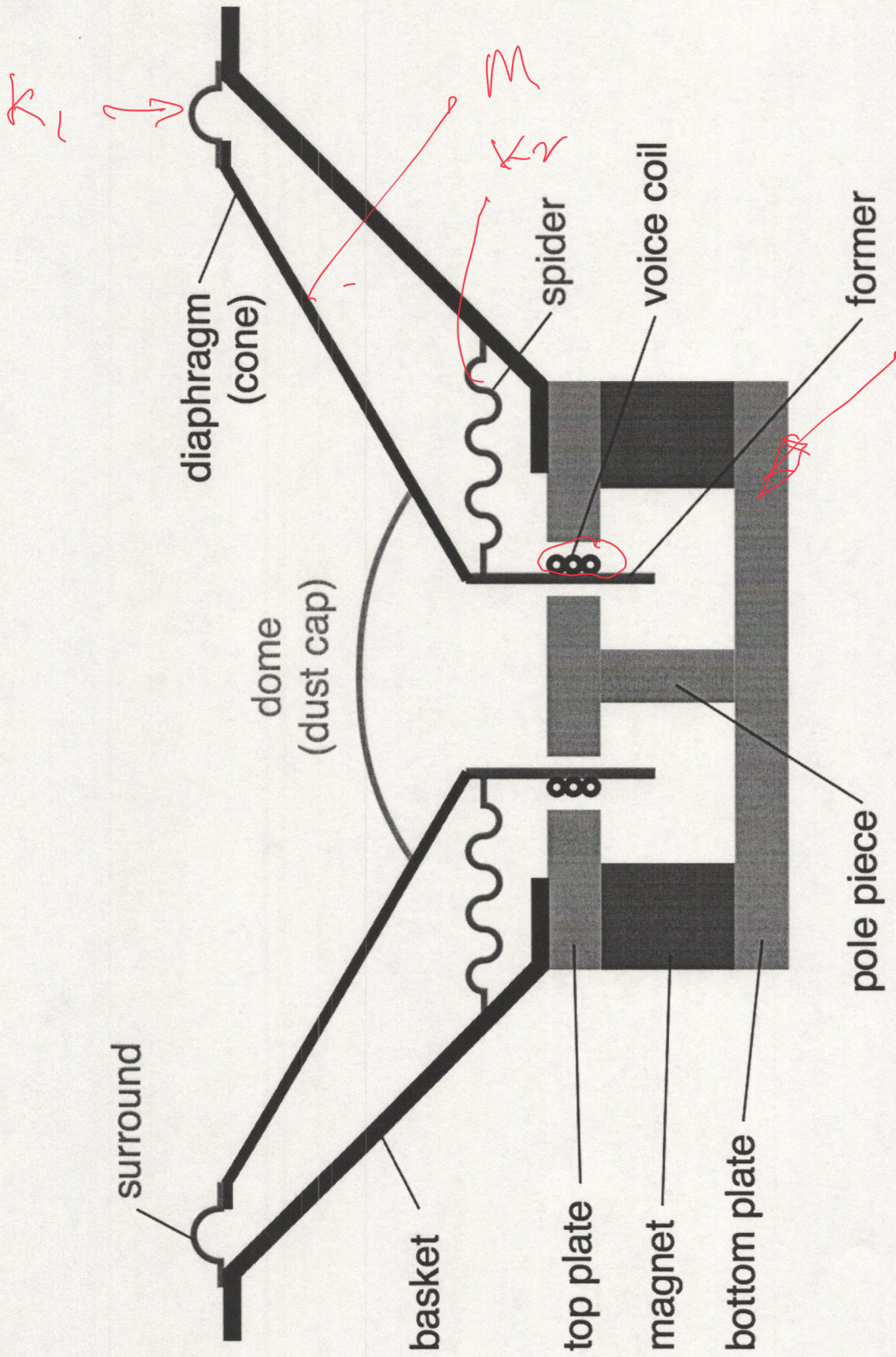


$$CA = \frac{V}{\rho_0 c^2}$$

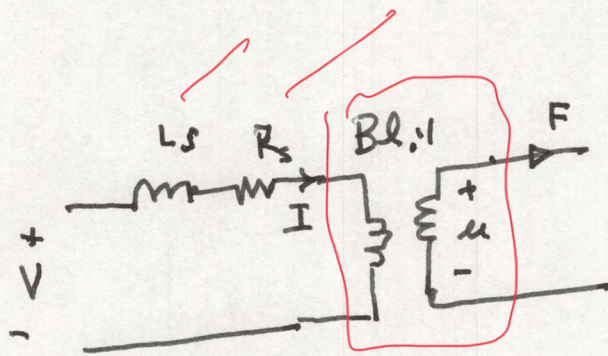


$$MA = \frac{\rho_0 l}{A}$$





$$I B l = F$$

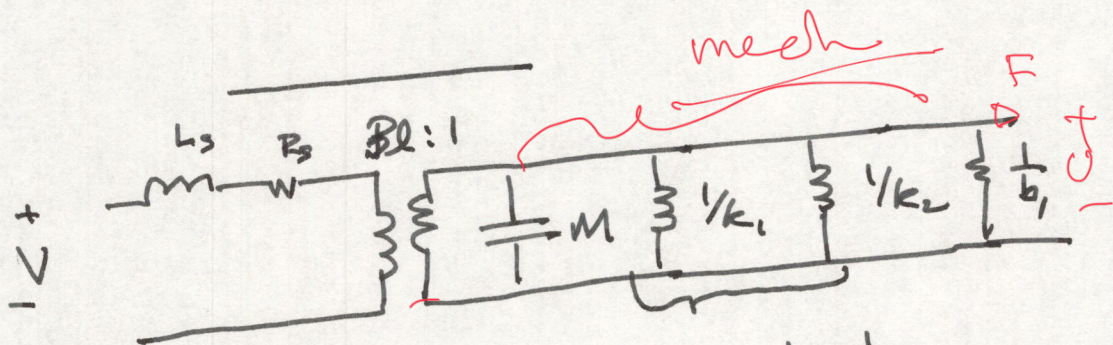
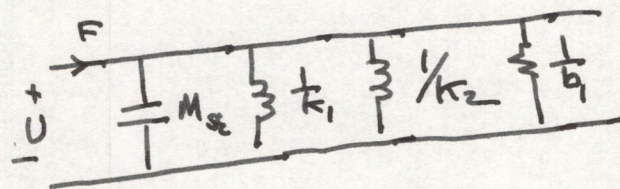


electrical

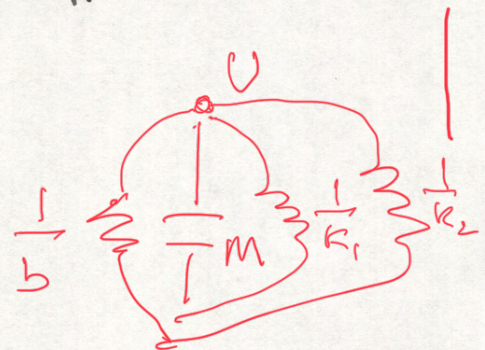
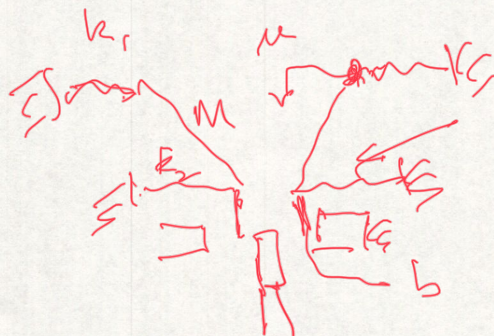
$$F = B l I$$

$$U = \frac{1}{B l} V$$

Consider the mechanic elements

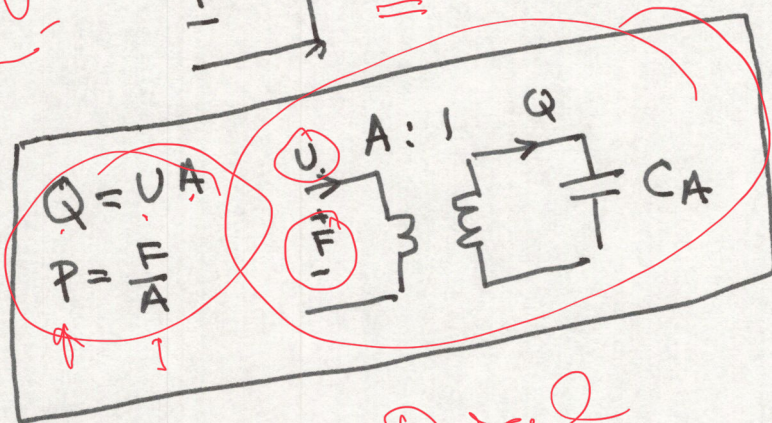
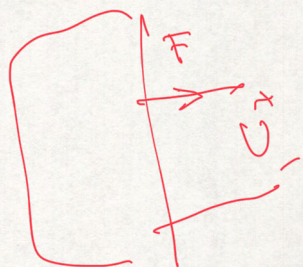
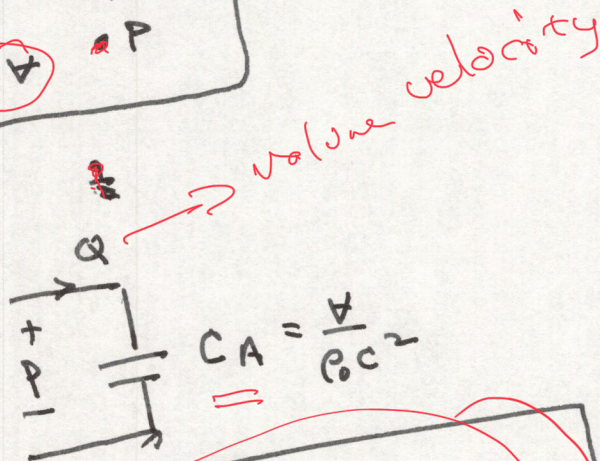
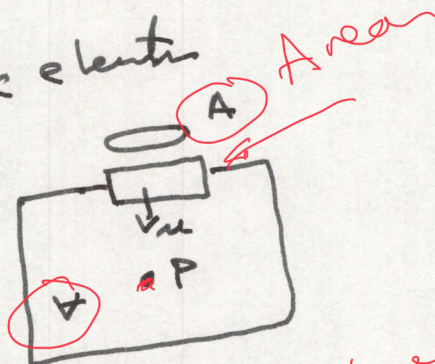


$$\frac{1}{k} = \frac{1}{k_1} \parallel \frac{1}{k_2}$$

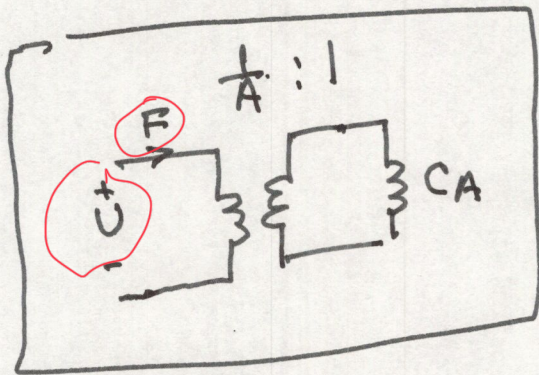
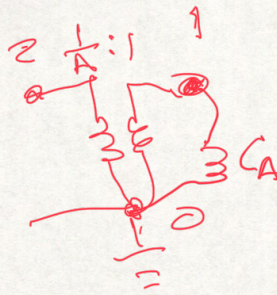
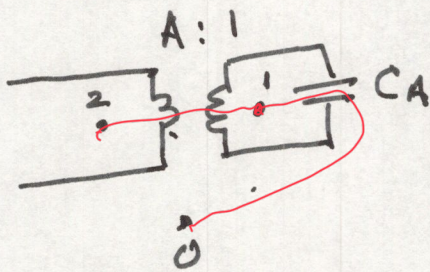


Speaker in a cab

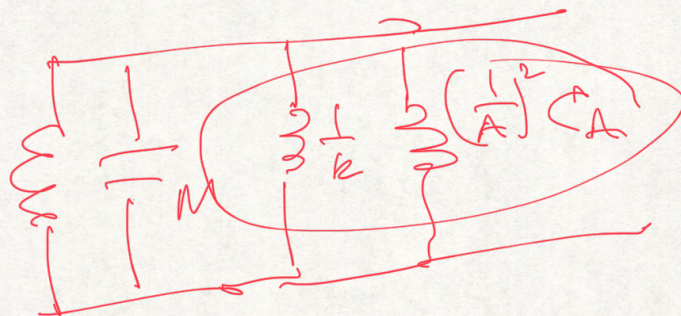
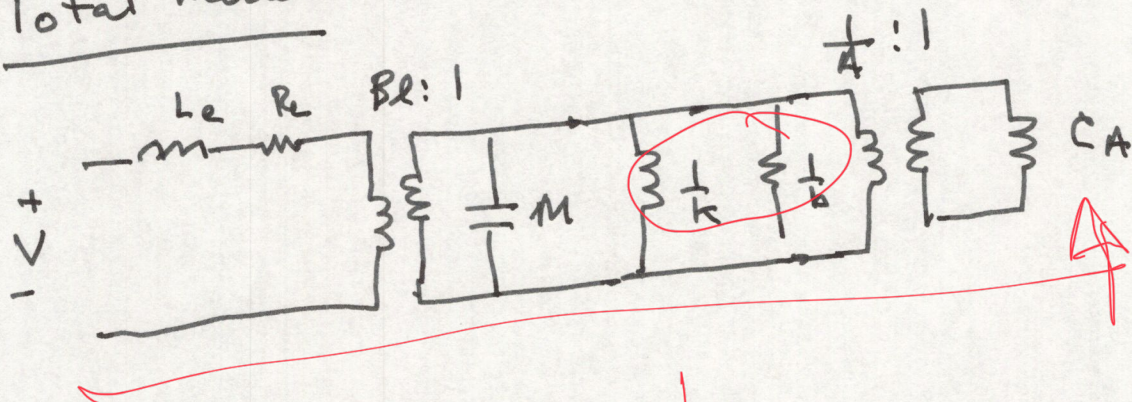
Acoustic element



Dual

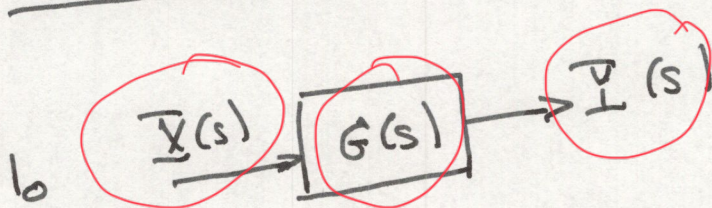


Total model



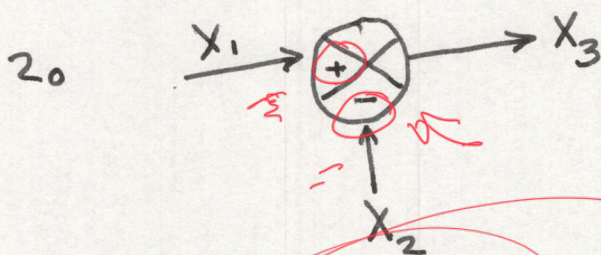
Representation of System

Block Diagram //



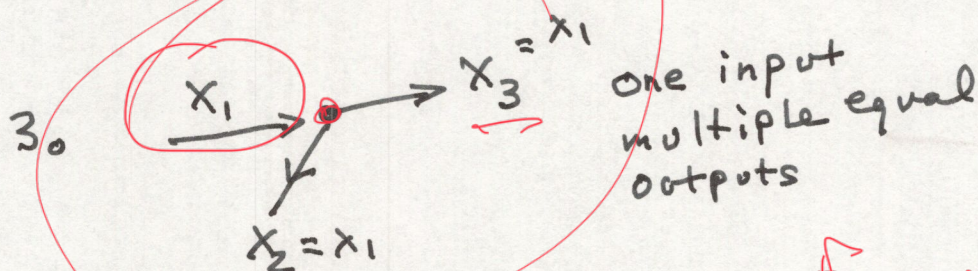
Basic system unit

$$Y = GX$$



$$X_3 = X_1 - X_2$$

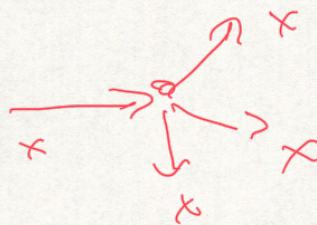
Summing junction



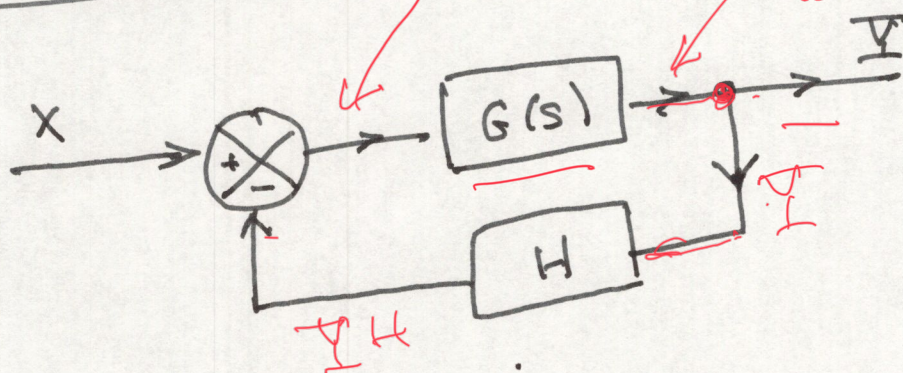
one input multiple equal outputs

Fan out

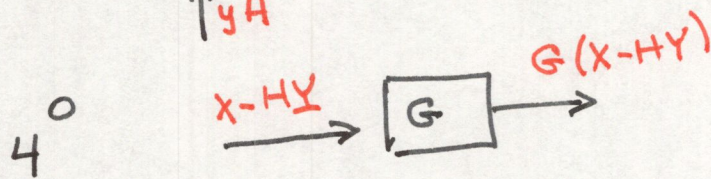
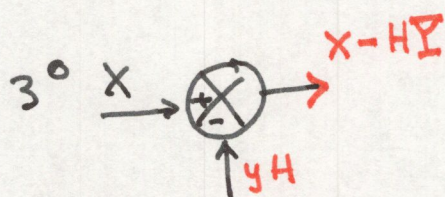
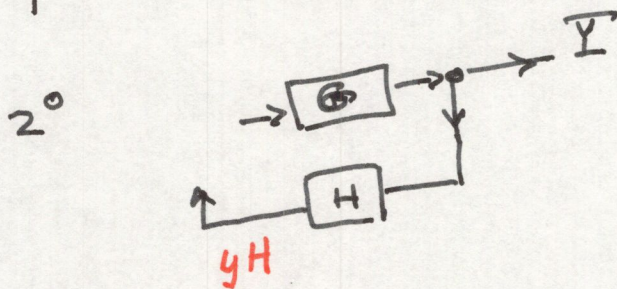
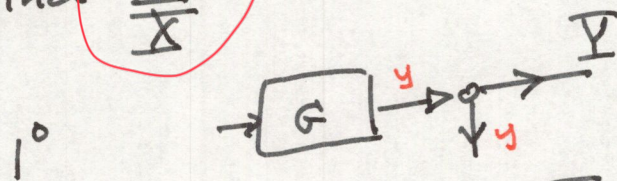
$$\begin{aligned} X_2 &= X_1 \\ X_3 &= X_1 \end{aligned}$$



Consider



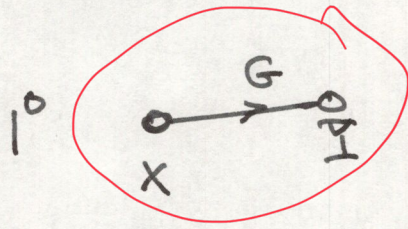
Find $\frac{Y}{X}$



5° $G[X - HY] = Y \Rightarrow GX = Y[1 + GH]$

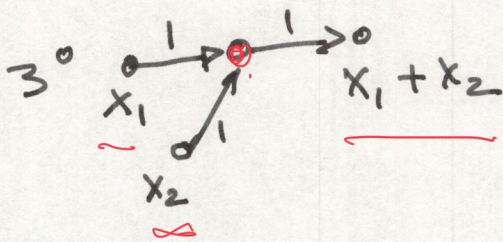
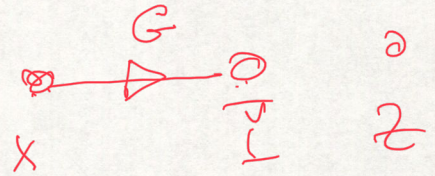
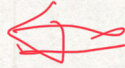
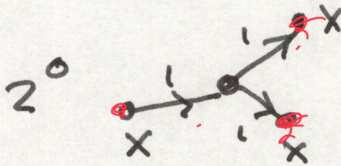
$$\boxed{\frac{Y}{X} = \frac{G}{1 + GH}}$$

Signal Flow Graph ~~g~~



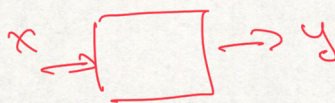
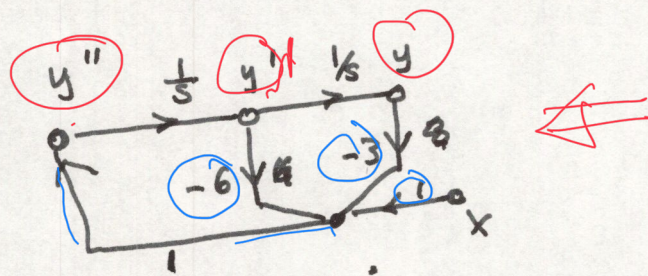
$$\underline{\underline{XG = Y}}$$

nodes
edge



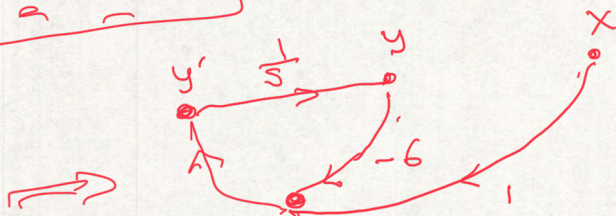
Consider

$$y'' + 6y' + 3y = x \Rightarrow y'' = \underline{\underline{-6y' - 3y + x}}$$



$$y' + 6y = x$$

$$\boxed{y' = x - 6y}$$

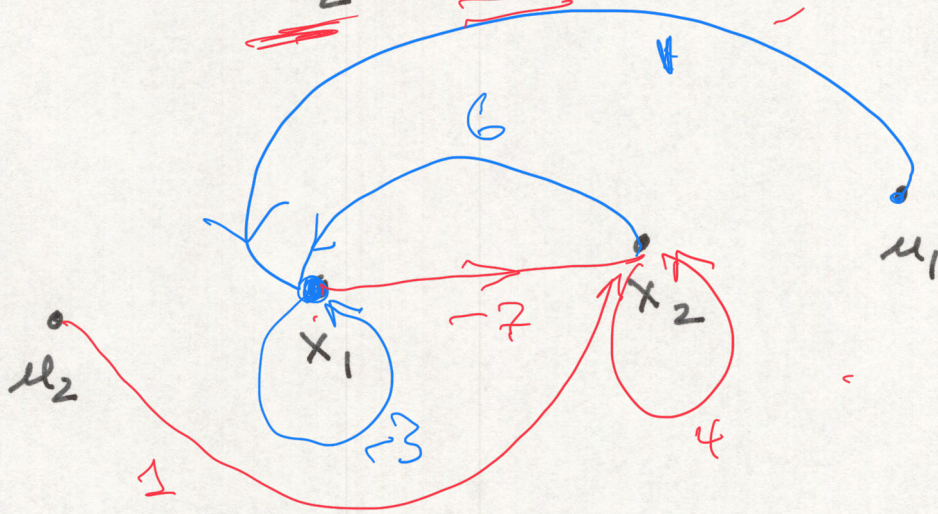


$\left(\frac{1}{s}\right) \Rightarrow$ Integrator

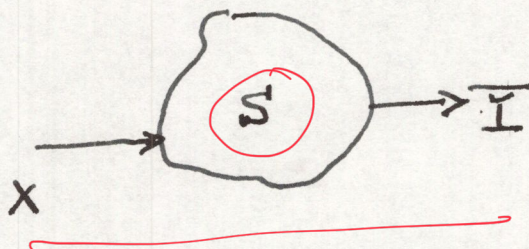
$\frac{1}{s} \Rightarrow \frac{1}{s} \cdot \frac{1}{s} = \frac{1}{s^2}$

$$\Rightarrow x_1 = 6x_2 - 3x_1 + u_1$$

$$\Rightarrow x_2 = -7x_1 + 4x_2 + u_2$$



⇒ Mason's Gain Formula



$$\frac{Y}{X} = \frac{\sum_i \Delta_i P_i}{\Delta}$$

1° P_i forward path gains from X to Y

2° Δ graph determinant

$$\Delta = 1 - \sum_i L_i + \sum_i L_i L_j - \sum_i L_i L_j L_k + \dots$$

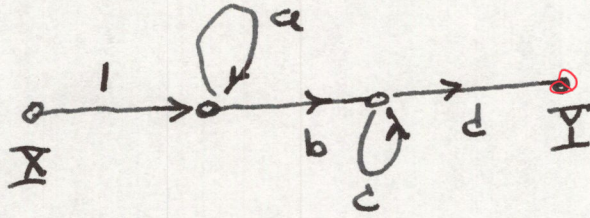
↑
non touching loop

⇒ 3° Δ_i cofactor after removal of touching loop

~~loop~~ P_i

$$\Delta_i = 1 - \sum_j L_j + \sum_j L_j L_k - \sum_j L_j L_k L_m$$

example



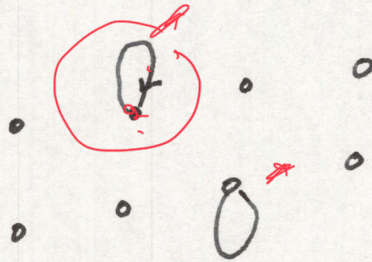
Find $\frac{Y}{X}$

$$\Delta = 1 - [L_1 + L_2] + [L_1 L_2]$$

FP



Loops:



$$L_1 = a$$

$$L_2 = c$$

touch P_i
a c

$$\Delta_i =$$

$$\Delta = 1 - (L_1 + L_2) + L_1 L_2$$

$$\Delta_i = 1$$

$$\frac{Y}{X} = \frac{P_i \Delta_i}{\Delta}$$